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NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

TECHNICAL NOTE

No. 1716

TABLES OF HYPERGEOMETRIC FUNCTIONS FOR USE IN

COMPRESSIBLE-FLOW THEORY

By Vera Huckel

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Langley Field, Va.



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Errata

Pages 10 and 11: The captions for table 3 and table 3 concluded should read:

THE FUNCTIONS $-\frac{2}{\beta k}\frac{dY_k}{d\tau}$ FOR AIR ($\gamma=1.4$) FOR SEVERAL VALUES OF THE INDEX k

Pages 12 and 13: The captions for table 4 and table 4 concluded should read:

THE FUNCTIONS $-\frac{2}{\beta k} \frac{dY_{-k}}{d\tau}$ FOR AIR ($\gamma = 1.4$) FOR SEVERAL VALUES OF THE INDEX k

Addenda

For completeness the additional formulas of reference I used in the computation of the functions are as follows:

For arbitrary positive indices

$$Y_k(\tau) = F(a_k, b_k, k+1; \tau)$$

For negative nonintegral indices

$$\overline{Y}_k(\tau) = \tau^{-k} F(a_k-k, b_k-k, l-k; \tau)$$

where

$$a_k + b_k = k - \beta$$

$$a_k b_k = -\frac{k}{2} (k + 1)\beta$$

and

$$F(a, b, c; \tau) = 1 + \frac{ab}{c} \tau + \frac{a(a+1)b(b+1)}{2! c(c+1)} \tau^2 + \cdots$$

For negative integral indices
$$Y_{-k}(\tau) = 1 - \frac{\left(a_k - k\right) \left(b_k - k\right)}{1! \ (k-1)} \ \tau + \frac{\left(a_k - k\right) \left(a_k - k+1\right) \left(b_k - k\right) \left(b_k - k+1\right)}{2! \ (k-1)(k-2)} \ \tau^2$$

$$- \frac{\left(a_k - k\right) \left(a_k - k+1\right) \left(a_k - k+2\right) \left(b_k - k\right) \left(b_k - k+1\right) \left(b_k - k+2\right)}{3! \ (k-1)(k-2)(k-3)} \ \tau^3 + \dots$$

$$3! \ (k-1)(k-2)(k-3)$$

$$+ (-1)^{k-1} \frac{\left(a_k - k\right) \left(a_k - k+1\right) \dots \left(a_k - 2\right) \left(b_k - k\right) \left(b_k - k+1\right) \dots \left(b_k - 2\right)}{(k-1)! \ (k-1)!} \ \tau^{k-1}$$

$$+ c \left[\tau^k \ F\left(a_k, b_k, k+1, \tau\right) \log \tau + \frac{a_k b_k}{1! \ (k+1)} \left(\frac{1}{a_k} + \frac{1}{b_k} - \frac{1}{1} - \frac{1}{k+1}\right) \tau^{k+1}$$

$$+ \frac{a_k \left(a_k + 1\right) b_k \left(b_k + 1\right)}{2! \ (k+1)(k+2)} \left(\frac{1}{a_k} + \frac{1}{a_k + 1} + \frac{1}{b_k} + \frac{1}{b_k + 1} - \frac{1}{1} - \frac{1}{2} - \frac{1}{k+1} - \frac{1}{k+2}\right) \tau^{k+2} + \dots$$

and

$$c = (-1)^{k+1} \frac{(a_k - 1)(a_k - 2) \dots (a_k - k)(b_k - 1)(b_k - 2) \dots (b_k - k)}{k! (k - 1)!}$$



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COMPRESSIBLE-FLOW THEORY

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SUMMARY

In the hodograph method of treating plane potential compressible flows the differential equation, originally obtained by Chaplygin in his study on gas jets, plays a significant role. This paper tabulates various hypergeometric functions which arise as particular solutions of Chaplygin's differential equation. The tables should prove useful in the tabulation of other auxiliary functions which may arise in various compressible-flow problems. The adiabatic index for air has been taken as 1.4.

INTRODUCTION

Any general theory of compressible potential flow will probably involve the hodograph variables. A reason for this statement is that in the hodograph plane, in which the independent variables are the magnitude and the direction of the fluid velocity, the equations of motion are linear; whereas, in the physical plane they are in general an intractable set of nonlinear partial differential equations.

The simplification due to the use of hodograph variables, however, presents certain difficulties which do not appear in the physical plane. For example, application of the necessary boundary conditions for uniform compressible flow past an arbitrary body is almost impossible, at least up to the present time. Certain singularities in the flow also appear, notably, near the sonic speed and in the undisturbed flow at infinity. Nevertheless, the possibility of getting around these and other difficulties in the near future justifies the publication of tables for the fundamental set of functions which represent the particular solutions of the flow equations in the hodograph plane.

The following section contains equations and definitions necessary for the understanding of the several functions listed in the tables. The reader is referred to the original paper (reference 1) in which the particular flow solutions are derived in detail.

EQUATIONS AND DEFINITIONS

The linear equations in the hodograph variables θ and q, which relate the velocity potential ϕ and the stream function ψ for the steady two-dimensional flow of a nonviscous compressible fluid, are

$$\frac{\partial \vec{d}}{\partial \vec{Q}} = -y^{5}(\vec{d}) \frac{\partial \vec{Q}}{\partial \vec{A}}$$

$$\frac{\partial \vec{Q}}{\partial \vec{Q}} = y^{T}(\vec{d}) \frac{\partial \vec{Q}}{\partial \vec{A}}$$
(1)

in which, for the adiabatic equation of state between the pressure and density,

$$\lambda_{1}(q) = \frac{\rho_{0}}{\rho}q$$

$$= \frac{q}{(1 - \tau)^{\beta}}$$

and

$$\lambda_{2}(q) = -q \frac{d}{dq} \left(\frac{\rho_{0}}{\rho q}\right)$$

$$= \frac{\rho_{0}}{\rho q} (1 - M^{2})$$

$$= \frac{1 - (2\beta + 1)\tau}{q(1 - \tau)^{\beta + 1}}$$

where

- q magnitude of fluid velocity
- θ angle included by velocity vector and positive direction of x-axis
- ρ density of fluid
- a velocity of sound in fluid
- M Mach number (q/a)

$$\beta = \frac{1}{\gamma - 1}$$

y ratio of specific heats at constant pressure and at constant volume, taken as 1.4 for air

$$τ$$
 dimensionless speed variable $\left(τ = \frac{q^2}{2βa_0^2} = \frac{M^2}{2β + M^2}\right)$

The index o refers to stagnation point q = 0.

Observe that the Mach number is given in terms of $\ensuremath{\tau}$ by the relation

$$M^2 = \frac{2\beta \tau}{1 - \tau}$$

For the tables the numerical value $\beta = 2.5$, corresponding to $\gamma = 1.4$, is used. Hence

$$M^2 = \frac{5\tau}{1-\tau}$$

and M = 1 corresponds to $\tau = \frac{1}{6}$.

By substituting in equations (1) the product-type solutions

$$\phi_{\mathbf{k}} = P_{\mathbf{k}}(\mathbf{q}) \underset{\text{sin}}{\cos} (\mathbf{k}\theta)$$

$$\psi_{\mathbf{k}} = Q_{\mathbf{k}}(\mathbf{q}) \underset{\text{cos}}{\sin} (-\mathbf{k}\theta)$$
(2)

and by observing that from equations (1)

$$kP_{k}(q) = \frac{\rho_{o}}{\rho} q \frac{dQ_{k}(q)}{dq}$$

$$\frac{dP_{k}(q)}{dq} = -kq \frac{d}{dq} \left(\frac{\rho_{o}}{\rho q}\right) Q_{k}(q)$$
(3)

the functions $Q_k(q)$ can be shown to satisfy the following second-order differential equation:

$$q^{2} \frac{d^{2}Q_{k}}{dq^{2}} + (1 + M^{2})q \frac{dQ_{k}}{dq} - k^{2}(1 - M^{2})Q_{k} = 0$$
 (4)

The functions $P_k(q)$ can be obtained from $Q_k(q)$ by means of the first of equations (3). Equation (4) may be reduced to a standard type by the introduction of the dimensionless speed variable τ as the independent variable. Thus, let

$$Q_{k}(q) = q^{k}Y_{k}(\tau)$$
 (5)

where clearly $Y_k(\tau) \to 1$ as $\tau \to 0$ (incompressible case). After some elementary operations the desired differential equation is

$$\tau(1-\tau)\frac{d^{2}Y_{k}}{d\tau^{2}}+\left[(k+1)-(k+1-\beta)\tau\right]\frac{dY_{k}}{d\tau}+\frac{1}{2}\beta k(k+1)Y_{k}=0 \quad (6)$$

Equation (6), which is of the hypergeometric type, was first introduced by Chaplygin in his memoir on gas jets (reference 2).

In the present paper, tables of numerical values have been prepared for a selected number of the complete set of particular solutions of equation (6). These solutions extend the results of Chaplygin into the supersonic range and to negative values of the index k.

DESCRIPTION OF TABLES

Tables 1 and 2 have been prepared for the functions Y_k and tables 3 and 4 for the functions $\frac{dY_k}{d\tau}$ for both positive and negative values of the index k ranging from 0.5 to 15 in increments of 0.5 and for the speed variable τ ranging from 0.01 to 0.50 in increments of 0.01. The critical value of τ is 1/6 for air; hence the present tables extend considerably into the supersonic range. Thus, corresponding to the value τ = 0.50, the Mach number is $\sqrt{5}$.

For large values of the index k (for example, greater than 15), it is possible to develop and utilize asymptotic expressions which involve the function $h(\tau)$ for M <1 (see discussion following equation (42) of reference 1) and involve the function $\theta(M)$ for M >1 (see equation (57) of reference 1).

The numerical evaluation of the functions listed in the tables was performed with both manual computing and with the aid of an IBM computing machine. The tables may be considered accurate as listed although the actual computations made full use of the capacity of the machine and involved many more places.

It is hoped that the tables presented in this paper will be found adequate and useful for the numerical evaluation of auxiliary functions which may arise in the solution of problems of compressible flow.

Langley Aeronautical Laboratory
National Advisory Committee for Aeronautics
Langley Field, Va., May 20, 1948

REFERENCES

- 1. Garrick, I. E., and Kaplan, Carl: On the Flow of a Compressible Fluid by the Hodograph Method. II Fundamental Set of Particular Flow Solutions of the Chaplygin Differential Equation. NACA Rep. No. 790, 1944.
- 2. Chaplygin, S. A.: On Gas Jets. (Text in Russian.) Sci. Ann.,
 Moscow Imperial Univ., Math.—Phys. Sec., vol. 21, 1904, pp. 1-121.
 (Available as NACA TM No. 1063, 1944.)

TABLE 1.- THE PUBLICATIONS Y_k FOR ALE (7 = 1.4) FOR

SEVERAL VALUES OF THE INDEX &

ж -	7	Y0.5	Y _{1.0}	Y1.5	T2.0	Y2.5	Y3.0	Y3.5	¥4.0	¥4.5	¥5.0	¥5.5	¥6.0	¥6.5	¥7.0	¥7.5
0.22473 .31944 .39324	0.01 .02 .03	0.99377 .98760 .98047	0.98756 .97525 .96306	0.96138 .96300 .94487	0.97522 .95087 .92695	0.96909 .93807 .90932	0.96303 .92700 .89198	0.95695 .91527 .87495	0.95093 .90369 .85822	0.94495 .89224 .841.80	0.93900 .88093 .82568	0.93309 .86976 .80986	0.92722 .85873 .79434	0.92138 .84783 .77911	0.91558 .83708 .76416	0.90981 82645 74950
.39324 .45644 .51299	.04 .05	-97539 -96935	939099	.92699 .90936	.90346 .88039	.88043 .85820	.85792 .82481 .79262	.83594 .79823	.81449 .77245	79357 74747	.77316 .72326 .67588	.75326 .69981 .64938	.73386 .67710	.71195 .69311 .59938	69651 63383 .57581	.67855 .61322
.51299 .56493 .61347 .65938	.06 .07 .08	.96337 .95743 .95154	.92723 .91554 .90396	.89197 .87482 .87791	.83549 .83546	.82461 .79766 .77135	.76135 .73098	76178 72656 69255	.73205 .69325 .69600 .62027	70343 66139 62129	.63094 .58834	.601.84 -55707	62389 57405 52742 48384	54752 49932 45457	.5 <u>2218</u> .47268	.55316 .49800 .44743
70321 74536	.09	94970 93990	.89251 .88117	.85791 .84124 .82460	.79224 .77122	74565 72057	.70149 .67286	.62804	.62027 .58600	.58306 .54663	.54798 .50979	.51495 .47534	.48984 .44315	.45457 .41309	.42704 .38503	.40114 .35883
.7861a .82572	.17 31.	.93415 .92845	.86996 .85886	.80861 .79265	.75060 .73037	.69609 .67220	.61508 .61813	.59748 .56803	.55316 .59171	.51195 17895	.1:7367 .43955	. 43815 . 40326	.405 <u>21</u> .36987	.37469 .33917 .30639	.34641 .31097 .27649	.32022 .26506
90219 9393	:13	.92279 .91719	.81789 .83703 .82629	79265 77692 76142	.71073 .69107	.64891 .62619	.56668	.53965 .53999 .48601	.59171 .49160 .46980	14739 14779	40733 37695	.37056 -33994	.33699 .30645	.27616	.24879	.25308 .22107
·97590	.15 .16	.91162 .90611 .90064	.81.567	.74615 .73111 .71630	67200 67331 63499	.60405 .58246 .56143	.54e15 .51838	.46070	.43526 .40896 .38384	.38951 .36268 .33726	.34832 .32138 .29604	.31132 .88458 .25965	.27811 .25185 .22755	.24633 .22276 .19930	.22166 .19694 .17445	.19779 .17404 .15263
1.0120 1.0476 1.0830	.17 .18 .19	-89522 -88984	.80517 .79479 .76452	.70171 .68734	.51705 .59947 .58225	.54095 .52101	.49537 .47310 .45156	.43635 .41296 .39049	35986 3370	.31319 .29043	27225 24992	.23641 .21480	.20511 .18441	.17781 .15817	.15404 .13555 .11884	.13336 .11607
1.1190	-20	.88451.	.77436	.67320	1	.50159 .48270	.43073 .41060	.36892 .34822	.33527	.26892 .24860	.22900 .80941	.19472	.16535	1939	.10377	.10059 08678
1.1529 1.1875 1.2221	.gz.	.87923 .87399 .86879	.76432 .75440 .74429	.67928 .6757 .63208	.56539 .54889 .53273	.46432 .44644	39115 37237	.32837 .30936	.27485 .27485	.22945	.19110 .17401	.19863 .14288	.13176	.10912	.09022 .07807	.07448 .06357
1.2221 1.2566 1.2910	: 82 53	.86879 .86364 .85854 .63348	73489 72533	61881 60576	.51693 .50146	.42907 .41218	.35425 33676	.29115 .27372	.23834 .22047	.19441 .17845 .16345	.15807 .14324	.1281.5 .11457 .10208	.10360 .09134 .08018	.08354 .07259 .06274	.05720 .05751 .0880	.05393 .01513 .03798
1.3254 1.3599 1.3944	.26 .27 .28	184847	.71584 .70648 .69723	99291 58028 56785	.48634 .471.55	.39577 .37983 .36436	.31990 .30365 .28800	.25706 .24113 .22593	.20547 .19033 .17601	.13623	.12945 .11665 .10479	.09062	07005	.05391 .04602	.03128	. 03146 . 02580
1.4291 1.4638	.29	.84350 .83857 .83369	.69723 .6881.0 .67907	.57564 .54362	.45709 .44296 .42916	34935 -33479	.27293 .2584	-91142 -29758	.16247 .14969	.12392 .11242	.09382	.07053 .06178	07263	.03899 .03275	.02866	.02668
1.4988	.31, .32	.82886 30498	.67016 .66135	.5318a	.41567 .40250	.32067 .30698	.24450 .23110	.18440	.13764 .12629	.10169 .09171 .08243	.07\37 .06579	.053 <u>82</u> .04660	.03852 .03255	.02724	.01901 .01513	.01307 .01001
1.5339 1.5693 1.6049	-33	.81931 .81461	.65265	. 52021 . 50881 . 49760	.38964 .37708 .36483	.29372 .28068	.21624 .20589 .19405	.15993 .14860	.11562	.07382	.05079	.01007 .03118	.02724 .02253	.01815	.00180	.00744 .00529
1.6408	.35 .36 .37	.80995 .80533 .80076	.63558 .62721 .61894	.48660 .47979 .46517 .45475	.36463 .37288 .34123	.2684 .25641 .24478	71/195	.13764 .12764	.09618 .08737 .07918	.06585 .05848	03817 03817	.02890 .02416 .01994	.01837 .01472	.01125 .00850 .00615	.00694 .00452 .00284	.00351 .00206
1.7136 1.7506 1.7879	38 38	79623	60273	.44472	.32907 .33,879	23353 22266	.161 12 .151 17	.11798 .10884 .10020	.07142	.05169 .04543 .03969 .03443	.02782	.01620 .01289	.01153 .00676 .00637	.00\17 .00251	.00147 .00035	00001 00071
1.8257	.39 .40	.791.74 .78729	.59478	.43447	.30800	.21217	.1/1196	.09204	05756		.01940	.00998	.00260	.00002	00051	00123
1.8640 1.9028 1.9421	.41 .42	.78289 .77853	.58693 .57919	.42462 .41495 .40547	.29749 .28725 .27729	.20204 .19227 .18284	.13288 .12421 .11595	.08435	05035 04560 04027	.02963 .02526 .02130	.01267	.00724	.00200	0002	00169	00184
1.9821 2.0226	.43 .44 .45	.77462 .76994 .76971	.57155 .56401 .55658	.39616 .38704 .37610	.27729 .26760 .25817	.17377 .16508	.11595 .10809 .10061	.07030 .06390 .05791	03535	.01771	.00737	.00174 .00038	00101	7.00209 00247	00227 00239 00243	00202
2.0638	.46 .47	.7615e	.99698 .54925 .54202 .53488	.37810 .36934 .36075	24900 24008 23142	.15660 .14831 .14073	.09349 .06674 .08033	.05229 .04705 .04216	.02666 .02285 .01937	.01158 .00899 .00669	.00331 .00169 .00030	00075 00167 00242	00238 00283 00314	00272 00286 00291	00243 00240 00232	00193 00182 00167
2.1483 2.1918 2.1918	.48 .49	75326 74919 74516	.52785 .52092	-35233 -34409	.22301 .21484	13325	.0033 .0033	.03760	.01620	.00267	- 00088 - 00185	00299 00342	- 00334 - 00343	- 00289 - 00281	00219	- 00151

TABLE 1.- THE PERCYICES X_k FOR AIR $(\gamma=1.4)$ FOR SEVERAL VALUES OF THE IRDEX k - Concluded.

ĸ	т	Y8.0	¥8.5	Y9.0	Y9.5	¥10.0	¥10.5	¥11.0	¥11.5	Y12.0	T12.5	T13.0	113.5	Y14.0	Y14.5	¥15.0
0.22473	0.01	0.90408	0.89839 .80560	0.89273	0.88711	0.88152	0.87597	0.87045	0.86496	0.89992	0.85410	0.84872	0.84337	0.83806	0.83278	0.82753
.315\L .39324 .b5644	-020	.83,596		79737	.70527	. <u>(1730</u> .68026	0.8 <u>1597</u>	· 77773 •65438	.74613	73666	.61738 86713.	.71.866	.7089€	-69993 -58246	.63164	.60226
3332	.03 .04	.73511 66104	.72100 .64398	.70716	.69378 61116		.66719	,65438	.64180	1 404	.61738	60551	9388 9568	.48287	.571.27 .47039	.56029 .45823
.53900	~~ i	.59328	.57398	.62736	-51700	-59538	.58000 .50280	.56502 .48642	.55042 .47057	.53619 .45523	.52234 .44039	.50884 42604	419300 41915	.39871	.38571	.45023
36493	.05	ASTES.	51045	-55530 -19034 -13139	53722 47101	.51972 .47844	Jukao	.41745	.40097	38515	36994	39934	31130	37/0	31487	.37313 .30244
61347	.07	.47492	45290	43189	.41185	39272	.43479 .37448	35708	31019	39166	30956	29516	.983.3	.32782 .26834	25585	.e4394
.51899 .56493 .61347 .65938	80.	42372	-40087	.379≒1	-35909	-33985	32164	30439	.28806	.27260	-29797	.eh412	.23101	.21860	.25585 .20686	-19574
.70321 .74536	.00	-37679	-35390	-33238	.31216	-29315	.27530 .23-77	25852	.24276	-22795	-21404	20098	.18871	.17719	.16636	.15520
•14030	ا س. ا	-331-39	.311.59	-29032	·27050	-29201.	-23477	.21871	-20373	-18978	.17677	.16469	.15336	.14284	-13304	.12391
.78612 .82572 .86436	.11	-297991	-27355	-25280	.23361	.21585	.199kk	.18426	.17023	.15725	14,527	.13419	.12395	.11449	.10574	.097 6 7
82572	12	.26127	144659	21940	.20103	.18117	.16872	.15455	77120	.12965	.32874	.10874	.09958	وروه.	.08350	.097 6 7 .07646
.00436	:끊	22995	20890	16975	-17233	.15649	7,600	.12901	.11712	.10631	09650	.08759	.07949 .06301	.07214	.06547	.05941 .04578
.90 <u>91</u> 9 -93934	.15	.20176 .17644	18164	.16349 .14029	.11713	.13238	21910	-10714	-09637	.08667	•0 <u>779</u> 4	.07008	.06301	05665	-05093	-04578
.97590	1.16	.15375	.15735 .13578	.11987	.12506 .10580	.111/6	.09932 .08236	.08849	.07882	-07021	.06252 .04978	.05567 .04388	.04957 .03867	.04413 .03407	.03929 .03008	.03197 .02645
.97590 1.0320	.17	13347	.11667	1019	.08904	09335	.06788	.07264	05168	.05647 .04508	.03932	.03428	.02986	.02605	.032270	.01078
1.0476	.18	.11539	.09979 .08493	.08666	.07453	.06436	105757	.059 <u>2</u> 4 .04796	.04137	.03568	03077	02652	.02286	01969	.01696	.01978 -01461
1.0830	.19	.09932 .0 05 07	.08493	.07258	.05199	-05292	.05557 .04515	-03851.	.03283	.02798		.08029	.01797	01470	.01250	-01063
1.1180	.20	.00507	.071.89	.06070	.05192	.05292 .04318	.03639	.03065	-02579	-02170	.02383 .018 24	.01533	.01988	·010g1	.00907	·0076ī.
1.1529 1.1875	.91	.07249	.06049	.05042	.04399	.03494	.02905	-02414	-0200H	.03.662	.01378	.01141	,00945	.00782	.00646	.0093k
1.107	.22	06140	09055	04357	03414	.02801	02295	.01879	01536	.01255	01034	.00835	.00680	00554	100450	.00 7 34 .00366
1.2221	.93	∙0 5 168		.03398	.02749	.02220	.01791	-01442	01160	.00931	-00747	.00598	-00478	-00382	.00305	-00243
1.2566 1.2910	.25	.okgnB	.03450	.02751	.02189	.01738	.01377	.01089	.00899	-00677	.00532 .00368	.00417	.00327	.03255	.00199	.00154
1.3254	.26	03979	.02811	.02202	.01720 .01331	.01340	.010+1	.00806	.00622	-00 1 79	.00368	-00281	,00 <u>2</u> 14	.001.63	.00123	-00095
1.3599	.97	.02938 .02386	.01801	-01359	01010	.01011 00750	.00769 .00 55 5	.00581	.00137 .00295	.00397	00152	.00180	.00133 .00075	.00097 .00052	.00070 .00035	00050
1.3500	.28	.01913	.01410	.01031 .00766	.00718	.00538	.00383	.00270	.00187	98100.	.00086	.00056	.00035	00021	.00012	.00005
1.4291	.99	-01510	-01081	-00766	00536	.00370	-00251	-00167	-00108	1.00067	-00040	-00021	.00009	.00002	00002	00005
1.4030	.30	.01170	.00809	.00551	.00367	-00239	.003.53	-00090	-00050	-0002¥	-00008	000001	00007	00009	00000	000010
1,4988	.31	.00884	.00585	.00377	.00234	.00139	.00076	.00035	.00000	00004	-:00012	~.00015	00016	00015	00013	00012
1.5339	.32	00616	00102	-00239	-00139	.00065	00021	00003	0000.6	00022	00023	00022	00030	00017	00014	00011
1.5693	-33	-00450	-00256	.00131	-00054	+00009	0000.6	- 0002B	00032	00032	00029	00025	00020	- 00017	00013	1- 00010
1.6049	.94 .35	.00290 .00163	00340	.00049 00012	00003	-,00030	00041	00043	00041	00036	00030	00024	00019	00015	0001	00008
1,6771	36	.00062	- 00017	00056	00069	00055	00056 00063	00051 00053	00049	00036 00034	00025	00029	00017 00014	00010	00009	00006 00004
1.7136	-37	00016	- 00067	00085	- 00085	- 00077	00064	00051	000H0	00030	00022	00015	00011	00007	00005	00003
1.7 7 06 1.7879	.38	00073	- 00101	00103	00093	00078	- 00062	00047	00035	00025	-,00017	00038	00008	00005	00003	00008
1.7879	:39	00115	- 00123	00JJē	00094	00075	00097	- 00041	00029	00020	00013	00008	00005	- 00003	00001	~.00001.
1.8857	-40	001A2	00134	00114	00091	00069	00050	00035	00024	00015	00009	00006	7.00003	00001	0	0
1.8640	.41	00159	00139	00111	000055	4.0006I	00043	00026	oom8	-400011	00006	00003	000a.	lo	٥	ا ا
1.9028	.42	00157	00137	~00105	00076	00053	00035	- 00022	00013	00007	- 0000	00003.	0.000	ŏ	.00001	ĭ.‱. I
1.9421	-43	00167	00130	00095	00066	000/4	00028	00016	00009	00004	00001	0	.00001	.000001	-00001	.00000
1.9821	1.44	00162	00121	00085	00096	00035	00021	00011	00005	00002	0	.00001	.000001	.00001	-000CD	.00001
2.0638	-45 -46	00153 00141	00109 00096	00073 00061	00046	- 00027	00014	00007	000002	10	.00007	·000005	-0000e	.0000a	-00000I	·00001
2.1097	.47	00127	00382	00000	00036 00027	00020 00013	00009	00003	0.00002	100002	.00002	.00002	*0000T	.00001L	.00001.	.0000
2.1483	.48	00112	00069	00039	00019	00005	00001	.00002	.00003	400003	.00002	.00002	.00001	.00001	"""	ادا
2.1918	1.49	00096	00056	00029	00012	00003	-00002	.00003	-0000h	.00003	.00002	-000002	.00001	.00001	ŏ	iŏ i
2.2361	.50	~.000B1.	00044	00320	00006	.00001	.00004	.0000	400004	.00009	.00002	.00001	.00001	10	آة	ا ة ا

Table 2.- the functions Y_{-k} for air $(\gamma=1.4)$ for several values of the index k

																		-
×	7	¥-0.5	Y-1.0	T-1.5	Y-2.0	Y-2.5	Y-3-0	Y-3.5	Y_4.0	Y4.5	T-5.0	T-5.5	Y-6.0	¥-6.5	Y-7.0	Y-7.5	Y_8.0	Y_8.5
0.22473	6.01	1.00621	1.01234	1.01809	1.02834	1.03377	1.04023	1.04634	1.05282	1.05936	1.06600	1.07271	1.07947	1.08629	1.09316	1.10007	1.10703	1.11404
-31944						1.07107		1.09870	1.11260	1.12595	1.11016	1.15444	1.16911	1.18398	1.19910	1 2143	1.22999	1.24575
-39324	-03	1.01844	1.03611	1.04982	1.09633	1.11393	1.1/154	1.15790	1.18160	1.20151	1.22485	1.24731	1.27139	1.29756	1 32064	1.34613	1.37229	1.39896
.39324 .4564	-ભ્	1.02444	1-0-755	1.06370	1.13347	1.15692	1.20400	1.22420	1.26215	1.28774	1.32332	1.35396	1 38993	1.42438	1.616	1.49929	1.53869	1.57875
.51299	-05	1.03038	1.05869	1.07629	1.17171	1.20202	1.2743	1.29744	1.32639	1 38608	1.43954	1.47738	1.52964	1.57175	1.62862	1.67915	1.73604	1.79207 2.04836
. 61347		1,03625	1.0 597 4	1.08763	1.21049	1.24773	1.372+8	1.37703	1.46612	1.59719	1.57780	1.62051	1.69775	1.79160	1.80043	1.89386	1.07kk7 2.26864	
-61347	.07	1.04203	1.00011	1.09770	1.24935	1.29331	1.43760	1.46207	1.59965	1.62233	1.7290	1.78635	1.90171	1.96123 2.20657	2.07570 2.38198	2.15143 2.46235	2.63886	2.36012 2.74303
.65938	.05	1.01779	1.09010	1.10577	1.20193	1.33805	1.22903	1.64361	1.73675	1.76026	1.93888 2.16941	1.97659 2.19223	2.15078	2,49865	2.76563	2.63727	3.11187	3.21542
.70321 .74536	I 'YZ	1.02340	1 11015	1 10116	1.26200	1.38136	1.70716	1.73720	2.07790	2.07035	2.43746	2.43262	2.02210	2.83171	3.24609	3.28593	3.72071	3.79685
14750	וייי ו	1.07500	رىسى,	TTRIMO	1.30232	1.42201	T. (E)170	T. 12 120	210[150	2101037	21-31-10	E 1-350C	2100210	,		3.20,3	3-12-12	3.13.02
.78612	.11	1.06460	1.11969	1.19794	1.39882	1.46147	1.83161	1.83049	2-27359	2.23813	2.74469	2.69625	3.26269	3.21749	3.84363	3.61553	-4 - 50372	4.50562
82372	. <u></u>	1-07007	1.12063	1.13203	1 13336	1.49733 1.52986 1.55872	1.93871	1.99177		2.41034	3.09145	2.97858	3.78203	3.64449	5.46489	4.42869	5.50226	5.35516
.86772 .86436	.13	1.07548	1.13778	1.13507	1.46637	1.52986	2.01673	2.00929		2.58316	3.47697	3 27401	4.35437	+ 10919	5.46489	5.12135	6.75730	6.14967
.90219	.14	1.08083	1.14648	1.13881	1 49769	1.558(2	2.17.11		2.94130	2.75229	3 89726	3.97481	5.07033 5.83648	4.60050	6.5168	5.88073	8.30180	7.47903
93934	1.15	1.08511	1.15193	11.11007	11.72710	11 503611	2.20151	2.16605	3.18243	8 91300	4.34908	3,87146	5.83648	5.102 kg	7.73785	6.68353	10.17026	8.71364
97590	.16	1.09133	1.16313	117677	11 55175	1.60430	2.36601	2.23193	3.42769	3.06029	4.82594	4.15279 4.40623	6.67493	5.59394 6.04921	9.12281	7.19155 8.26600	12.36275 14.86862	9.99967 11.25518
7 0150	-17	1.09648	1.17110	1.14299	1 50029	1.62058	2.46712	2.28735	3.67350	3.18900	5.32014	4.40023	7.57292		10.65523		17.64587	12.16800
1.0476	•끄러	1-1017	1.17003	1.14222	1.60374	1.63229	8.20370		3.91607	3.29390 3.36985	5.62255	4.61813 4.77118	8.51270 9.47162	6.43800 6.72640	19.30573 14.03106	8.93751 9.43705	20.63927	12.1000
1.0830	1 .73	1.30660	1.10032	1 74110	1.02203	1.63932 1.64158	2.03302	2.36116 2.37702	4.15148 4.37570	3.11188	6.32271 6.80907	4.85951	10.42232	6.87787	15.77370	9.68277	23.67688	13.19549 13.56709
1.1180	1 -20	T-1112(T+13223	+ <i>•</i> T23445	1.04477	1.04130	2.13900	5.21105	4.31510	3.41100	0.0001	***		4.0/10/	2011310	3100211		23.70107
1.1500	اده. ا	1.11648	1.00063	1.13706	1.66006	1.63903	0.81750	2.37742	4.58471	3.41533	7.26922	4.85975	11.33331	6.85438	17.46225	9.56573	26.66837	13.28949
1.1529 1.1875	.00	1.10133	1.20746	1.13403	1.67555	1.63166	2.88708	2.35149	177-50	3.37597	7.69010	4.76085	12.16949	6.61791	19.01955	9.05353	29.40679	19.15492
1.9391	.03	1.10610	1.91407	1.13045	1.68787	1.61947	2.94789	2.3285		3.2900	8.05838	4.54987	10.89311	6.13190	20.32951	7.99472	31,66990	9.99208
1.g566	.24	1.13085	1.22047	11.12629	1.69793	1.60252		2.27605	5.08129	3.15438	8.36067	4.21534	13.46466	5.36298	21.30981	6.32372	33.20820	6.47978
1.2910	.25	1.13559	1.22666	13.32961	1.70772	1.58059	3.01069	2.20968	5.19109	2.96651	8.58385	3.74772	13.84401	4.28255	21.64515	3.96624	33.75275 33.02663	1.56239
1.3254	.26	1.14013	1.23265	1.11643	1.71197	1,55467	3.07164	2.12328	5.26750	2.72167	8.73.536	3.13976	13.99164 13.86982	2.86848	21.02620	86484	33.02663	- 93353
1.3599	.27	1.14469	1 2384	1.11079	1.71460	1.72398	3.09173	2.01.888	5.30767	2.42786	6.74354	2.38684		1.10658	21.14697	-3.01566	30.75852	-13.0818
1.3944	1.28	1.11919	1.24103	1.10471	קונות.נו	1.48097	3-10064	1.89667	5.30911	2.97593	8.65785 6.44917	1.48733	13.44398	-1.00799	19.70948		26.69793	22 .80090
1.4291	-29	1.15363	1.24944	1.09023	1.71.77	12.44979	3.09614	1.75703	5.26973	1.6695		.14273	12.569	-3.46955 -6.26106	17.45009	-13.11336 -19.24725	20.63157 12.40018	-34.23866 -46.96123
1.4638	.30	1.15001	1.27107	1.09130	1.71103	1.40664	3.00100	1.60053	2.79789	1.21025	8.33005	74209	TT-20-25-	-0.20000	14.83(8)	-13.50	12.4000	-0.5002
1.4988	.31	1.16014	1.05060	1 .06k1k	1.70615	1.35970	3.05860	1.42785	5.06235	.700ki	7.63483	-2.05802	10.06924	-9.35346	10.09018	-25.98772	1.91461	-60.74520 -75.17496
1.5339	30	1.16661	1.06	1.07660	1.60928	1.30920	7.00111	1.23987	4.89213	11324	7.02006	-3.49571		-12.70549	4.96906	-33 .19905	-10.82812	75.17196
1.7693	1,33	1.17083	1.26922	1.06875	1.69015	1.25534	2 97230	1.03779	4.67787	- 45724	6.26436	-5.03761	5.91543	-16.26379		-40.70736		-89.72579
1.5339 1.5693 1.6049	1.31	17,17100	1.97373	11.06063	1.67913	1.19838		6221	1.41892	-1.09626	5.36873	- 6.66611	3.26340	-19.96341	-8.11521	-48.30278		
1.6408	1 .35	1.17910	1.27807	1.05225	1.66630	1.13855	2.01050	59-80	4.11633	-1.76832	4.33655	-8.35977	24786	-23-72677		-55.74331	-67-70330	-116.6088
1.6771	.36	1.18316	1.28224	J1.04367	1.66630 1.65170 1.63541	1.07610	2.75885	-35694	3.77132	-2.46727	3-17355	-10.09438 -11.84337	-3.10385	-27.47407		-62 76042		r127 4030
1.7136	-37	1.18716	1.28626	1.0348	1.635k1	1.01130	2.66639	יסטני.	3.38561	-3.100-2	1.88608	11.6337	1-0-72	-31 -10903		-69.06620	-101.21004	1-730-3335
1.7506	1.36	17.19111	1.29012	1.02505	וכדנס גון	.94440	2 - 56395	14442		-3.91832	1 .49029	Lrg.2700	-m.05090	-34 - 53293		-74 36207	-191.62699 -151.31005	
1.7879	1 39	1.19901	1.29369	11-01670	1.59806	1 .07769	2.45203	40475 66928		-1.69598				-37.64472 -40.34382		-78.34861 -80.73681	-141-31905 -159-49064	
1.8257	·*0	T-13000	155135	1 -00740	1.57714	• 00743	2.33119	00928	5.0000	-5.39085	-2.7000	L-10:00-178	לחוסליםד-		-02.40503			ومرمعادرت
1.8640	L.10	1.20266	1.3000	.90700	1.55482	.73380	2.20202	93630	1,48564	-6.11498	-k.gako8	-18,30287	-23.27186	-te.50351	-72.73591	-81.65819	-175-29327	-124.789A:
1.9038		1.206h0			1.5011	66174	2.06518	-1.20406	.93744	-6.82013	-5.93165	1-19.76383	-27.51002	-12.52351 -14.09386	-80.38733.	1-79.67936	-187.86430	-108.3333
1901		1.21010		97887	1 50629	58806	2.06518 1.92135	-1.47082	36763	-7.49805	-7.65672	-20.96662	-31.70526	-44.96469	-86.12924	-75.81093	-196.35998	-85.7079
1.9801		1.21375			1.48023	.52439	11.77125	1-1.73480	- 21942	-8.11058	9.38878	-21 97235	-35.6811)	 - 45.05835	-94.67 <u>16</u> 5		199.99135	
2.0226		1.21735		95950	1.45306	44038	1.61563	-1.99 1 28	മുമാ	-8.73982	-11.105/8	22.75.18	-39.37978	+4.31063	-99.73579	-60.73962	-198.06151	-22.4031
2.0638	1.46	1.22090	1.31582		1.52487		1.45529	-2.2475	-1.42663	-8.58816	-12.78388	-23.28194	-42.71378	12.67336	-103.05831		-190-00268	
2.1057		1.22410			1.39573		1.29100		-2.03707	1-9-77643	1-24-40078	P23-55271	1-45-59620	40.11668	-104-40522	1-32-6512	1-175-1259	61.4815
2.1483		1.92787		93026	1.367			-2.72881	근 선정	10-50-00	[-15-93307	P23.53149	1-17.97270	-30.63100	-103.2760	1-13-92508	-154 08656	100.7030
6.1918		1.23126		9207	1.3348	.31775 .07660	-92391	2.92367	-3.24658	10.27000 10.27000	1.17.22	-32.57030	-49. (UIOL	-32 -22923 -26 .94606	-100-42684 -94-85051		-126 01419 -91 55 277	
5.5367	1.70	1.23462	-· 32 57	. 27008	1.30327	1.00000	-78274	1-2·10000	-3-83555	נווצף.מרוז	טטאכם-סדר	1-22.70540	יעכין יעכין	-20.y=000	-34.02021	11.31847	31.332(1	200.3013
	_							·	•		-						NACA	-

NACA

TABLE 2.- THE FUNCTIONS Y_{-k} FOR AIR $(\gamma=1.k)$ FOR EXPERAL VALUES OF THE INDEX k - Concluded.

ж	T	Y-9.0	¥-9.5	Y-10-0	Y-10-5	Y-11.0	¥-11.5	Y-32.0	Y-12.5	¥-13.0	Y-13.5	T-14.0	Y-14.5	Y-15.0
0.22173 .31944 .39324 .47644 .76299 .61347 .67938 .70321 .74736	.07	1.12109 1.26173 1.42621 1.62030 1.6215 2.13375 2.15306 2.96571 3.50151 4.25830	1.12820 1.27792 1.45401 1.66283 1.91302 2.216595 2.56995 3.64048 1.37867	1.13534 1.25433 1.48239 1.70668 1.97720 2.30801 2.72131 3.24946 3.94256 4.87150	1.14253 1.31096 1.51134 1.71166 2.04273 2.39956 2.34336 2.40361 4.12018 5.04379	1.14977 1.32760 1.54087 1.79793 2.11119 2.498490 3.61220 4.44325 5.57405	1.15766 1.34487 1.57592 1.54542 2.59854 3.75283 3.75283 3.75283 3.75283 3.75283 3.75283	1.16439 1.362171 1.60171 1.69423 2.27487 2.70506 3.27669 4.01938 5.01237 6.38190	1.1717 1.37966 1.63304 1.5434 2.33046 2.33046 4.32197 5.37168 6.66867	1.17920 1.39740 1.66500 1.99580 2.40866 2.93004 3.79897 4.47610 5.69958 7.31014	1.4575 1.4575 1.4575 2.	1.1949 1.4338 1.7308 2.5738 2.57438 3.17438 3.9345 4.98795 6.39561 8.38040	1.20176 1.45201 1.76470 2.15863 2.65987 3.30409 4.1445 5.25861 6.76576 8.84686	1.4009 1.47009 1.47009 1.47009 2.43009 2.43009 2.43000 2.50017 7.22000 9.61427
.76612 .82772 .85436 .90219 .93934 .91290 1.0476 1.0630 1.1180	747 75558 98	5.26038 6.58282 8.30784 10.51724 13.28171 16.66743 20.62066 25.15160 30.15895 35.31635	5.30511 6.45212 7.64141 9.47404 11.31865 13.22916 15.26313 17.07262 18.32938 18.32988	6.13905 7.85083 10.17177 13.25610 17.25956 22.35764 28.46234 35.68367 43.76883 52.41374	6.23400 7.72292 9.65375 11.96329 14.65855 17.64160 20.70700 23.51973 25.59430 26.28858	7.14387 9.34325 14.64687 16.64687 28.77.3630 28.77.3630 26.42157 77.4672	7.31572 9.29718 11.85796 15.06779 18.93890 23.35289 28.00569 32.34833 35.52780 36.35926	8.31853 11.10378 15.11898 20.64427 28.82866 39.62988 53.65449 71.08834 91.57802 114.09781	8.7/6/1. 11.13201. 11.73208 18.937/1. 24.41820 30.8568 37.82088 14.42986 49.22273 50.06599	9.68601 13.18426 18.37894 26.03917 37.10348 52.58317 73.36916 39.92783 131.88685 167.54191	10.0498 11.12866 11.12866 11.12866 11.12865 11.02865 11.02865 11.0286	11.28133 15.64628 22.31221 32.46717 47.69058 69.6333 100.11537 140.18349 189.51619 245.36520	11.76987 15.90843 21.73571. 29.76409 40.39510 53.64562 68.73300 83.53502 93.99146 93.77512	13.14450 18.56319 27.06023 40.41914 61.08451 92.04344 136.36578 196.30570 271.80292 358.47985
1.1529 1.1875 1.2221 1.2566 1.2910 1.3254 1.3599 1.3594 1.4291 1.4638	ម្មនិងមន្តៃ មន្តៃ មន្តិ	40.44430 45.10502 48.00201 50.99235 51.01508 48.22157 41.96625 16.68675 16.68675 16.68675 16.68675		60.98180 68.68563 74.48708 77.14027 75.24094 67.30369 51.86633 27.61793 -6.47345 -50.91392	24.8179 20.27077 11.69838 -1.87743 -21.12407 -46.78018 -78.92492 -117.24766 -160.79144 -207.88361	91.49304 103.90450 112.96889 114.85431 107.73999 86.00604 52.50363 -1.50183 -17.93201 -171.46820	33,3320 8,46942 8,44996 -17,83790 -18,75987 -16,75987 -235,88788 -316,17195 -40,37081	-89.24659 -245.18664	44.13928 28.02983 -2.02392 -49.72297 -118.12998 -208.94776 -321.70675 -452.94976 -595.52039 -738.08664	203.34340 233.47719 249.70334 240.64604 194.09094 96.177198 -302.54760 -617.62386 -1007.24707	77.42443 28.05943 -26.54923 -113.53151 -238.47108 -403.88284 -607.27622 -639.24025 -1061.82940 -1307.61763	301.k312k 346.83287 365.k5082 335.9799k 233.04k36 29.63809 -298.9433k -769.76637 -1385.86504 -2129.46855	73 -02111 20 -54614 -77 -20349 -233 -28347 -457 -56292 -779 -07476 -1111 - 57609 -1508 -62341 -1901 - 81252 -2227 -25310	\$47.2802\$ \$12.19221 \$28.66693 \$37.60013 237.60678 -171.017\$4 -816.13337 -8267-74078 -4267.16683
1.4986 1.5339 1.5639 1.6649 1.6468 1.6771 1.7136 1.7506 1.7579 1.6257	.36 .37 .38	-27 . 57686 -27 . 576827 -50 . 576237 -128 . 573427 -168 . 60700 -209 . 51427 -200 . 51427 -270 . 51427 -287 . 57684 -320 . 58370 -346 . 31315	-128.5752 -137.82128 -137.82128 -204.31206 -222.30763 -233.49306 -237.8259 -227.8259 -227.8259 -226.8472 -178.61513	-170.08438 -242.36552 -320.00136 -339.48924 -476.43733 -545.68568 -601.50286	-256.08792 -302.21110 -302.21710 -312.15965 -386.82428 -381.5922 -352.01841 -294.35738 -206.00201 -85.90121	-287 .13107 -149 .90984 -56 .48809 -123 .11234 -857 .64704 -975 .68973 -1117 .10429 -1110 .00073 -1110 .48629	48 .05434 153 43153 164 .42755 163 .42653 163 .42667 164 .42667 165 .5667 165 .56	-674.95476 -934.600,76 -1205.91914 -1465.16693 -1667.97261 -1869.47599 -1801.97896 -1547.40309 -1102.89877	-111-03756 434-72034 1106-52053	-1476.28066 -1936.42773 -2407.14227 -2806.07367 -3071.24770 -3127.66477 -2893.66235 -2307.72142 -1317.39725 98.09661	-1479.80719 -1353.74239 -1480.08167 -1209.71071 -700.26787 -701.2572 1124.60600 2419.72124 3899.13591 2460.13001	-5786.60202 -4519.75595 -5010.69776 -5103.02542 -4632.16784	-2401.84593 -2328.17966 -1904.05672. -1005.49434 340.47158 2245.69421 4630.9042 7963.87065 10218.34547 12674.33337	9710-72290 -7042-04508 -7996-74136 -8256-42715 -7473-85696 -9327-73603 -1361-30503 3930-17013 11040-93968 19393-97410
1.8640 1.9028 1.9421 1.9621 2.0226 2.0638 2.1037 2.1483 2.1918 2.2361	.45 .46	-366, 20343 -366, 21647 -356, 31176 -330, 95064 -289, 14323 -253, 561335 -61, 76869 44, 06996 161, 03945	-61.34228 15-03145 103-43658 201.44780 305-77752 410-30463	477 74060 -341 89994 -165 65783	65.08246 243.86079 444.92726 660.30164 879.64071 1090.52396 1278.99233 1430.12568 1598.99037 1561.57261	-834 .88056 -557 .86488 -208 .17371 238 .96784 761 .18047 1338 .31908 1342 .76544 2540 .05406 3050 .17801 3549 .61274	1638.54210 2058.58761 2431.06979 2717.91017 2881.52277 2887.70234 2705.26342	387.84570 1409.83150 2568.03143 3800.54523 5025.84087 6145.86456	14867 - 81305 5203 - 148133 5200 - 15387 1781 - 75146	1921.74948 4089.34772 6484.57310 8937.19927 11229.85749 13107.19074 14294.63654 14722.06569 13772.52677 11212.76015	9045.55362 9223.90679 8565.58896 6920.03048 4204.64910 430.60433	9479.51060 14184.63576 18821.39155 22649.44729 25648.64806 26573.04584 25022.22079 20525.12465 12628.88453 1968.53129	14931.89167 15940.44769 15443.98517 13040.82665 6449.46586 1585.94414 17979.70301 17979.70301 189327.73393 140470.46470	26304.23061 36776.67337 43570.09131 47193.55448 46258.99836 39477.97789 25984.44439 25984.44439 25986.43124 21131.52198 22479.19996

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TABLE 3 THE PURPLICAS OF FOR AIR (7 = 1.4) FOR
SEVERAL VALUES OF THE DOORS. I:

							BAT ANTHE	OL THE TH								
×	Ť	40.5	811.0 47	4Y1.5	412.0	₫ <u>το.5</u> ₫τ	₫¥3.0 ₫₹	dr3.5	άΣ <u>μ.ο</u> ₫τ	dYb. 5	415.0 4.7	415.5	416.0 47	476.2	817.0 41	87.5 47
0.22473 .31944 .39324 .45644 .51299 .56493 .61347 .65936 .70321 .74536	0.01 .02 .03 .04 .05 .06 .07 .08	0.9923 .9845 .9768 .9692 .9615 .9739 .9463 .9367 .9311	0.9900 .9801 .9702 .9603 .9505 .9407 .9309 .9212 .9115 .9019	0.9866 .9734 .9602 .9471 .9340 .9211 .9082 .8994 .8827 .8701	0.9826 .9653 .9482 .9333 .9185 .8978 .8814 .8650 .8489	0.9781. .9564 .9350 .9359 .8930 .8725 .8322 .8322 .8124 .7930	0.9732 .9469 .9210 .8756 .8766 .8460 .8419 .7782 .7719	0.9682 .9370 .9065 .8475 .8190 .7911 .7638 .7372 .7111	0.9630 .9269 .8918 .8716 .8843 .7919 .7603 .7857 .6999	0.97[[.9166 .8769 .8363 .8010 .7619 .7899 .6961 .6339	0.9523 .9063 .8619 .8191 .7779 .7388 .7001 .6634 .6282	0.9468 .8958 .8469 .8001 .7772 .7122 .6710 .6317 .5941 .7782	0.9414 .8854 .8860 .7812 .7327 .6866 .6427 .6011 .5615 .5239	0.9359 .8750 .8173 .7625 .7107 .6617 .6153 .7115 .7302	25.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.	0.948 984 984 985 985 985 985 985 985 985 985 985 985
.76512 .82572 .80436 .90219 .93934 .97590 1.0120 1.0476 1.0630 1.1180	.11 .12 .13 .14 .15 .16 .17 .18 .19	.9160 .9035 .9010 .8936 .8961 .8787 .8713 .8540 .8966 .8993	.8923 .8327 .8732 .8637 .8343 .8449 .8355 .8262 .8170	.8576 .8327 .8327 .8304 .8082 .7961 .7840 .7721 .7602 .7454	.8170 .8013 .7858 .7704 .7552 .7462 .7253 .7105 .6959 .6815	.7737 .7348 .7361 .7177 .6996 .6817 .6641 .6168 .6297	.7296 .7076 .6860 .6648 .6040 .6236 .6366 .5840 .5649	.6877 .6608 .6366 .6330 .5899 .5674 .5435 .7251 .5033 .4830	.6426 .6127 .7890 .7632 .7383 .7341 .4907 .4679 .4460	.600.k -571.9 -7435 -7161 -4897 -4642 -4397 -4161 -3934 -3716	.5617 -5305 -5006 -4719 -4444 -4160 -3529 -3668 -3458 -3239	.7240 .4913 .4602 .4306 .4024 .3776 .3756 .3501 .3260 .3030 .2813	.4882 .4245 .4225 .3923 .3637 .3368 .3113 .2874 .2648 .2436	. 4545 . 1200 . 3875 . 3569 . 3665 . 3663 . 2763 . 2763 . 2763 . 2763 . 2763	.428 .387 .354 .354 .359 .269 .249 .220 .209 .163	.3930 .3776 .3249 .8457 .2405 .2167 .1947 .1745 .1560
1.1729 1.1875 1.2221 1.2766 1.2910 1.3274 1.3299 1.3944 1.4291 1.4638	.21 .22 .23 .24 .25 .26 .27 .26 .27 .28 .27	.8120 .8347 .8274 .8202 .8130 .8058 .7987 .7915 .7844 .7773	. 7985 . 7894 . 7802 . 7712 . 7621 . 7532 . 7532 . 7333 . 7264 . 7176	.7367 .7235 .7021 .6907 .6704 .6602 .6301	.6672 .6731 .6352 .7254 .6117 .5982 .5849 .5717 .5587	.5963 .5800 .5640 .5482 .5327 .5174 .5024 .4877 .4732 .4589	.5277 .5097 .4920 .4748 .4579 .4414 .4253 .4095 .3941 .3791	.4632 .4440 .4254 .4072 .2895 .3724 .3557 .3135 .3239 .3086	.4041 .3842 .3670 .3464 .3285 .3112 .2946 .2785 .2631 .2482	.3507 .3306 .3113 .2928 .2751 .2581 .2119 .2264 .2116	.3030 .2611 .2641 .2460 .3289 .2126 .1971 .1825 .1686 .1555	.2608 .2414 .2230 .2077 .1894 .1740 .1596 .1460 .1333 .1214	.2237 .2051 .1876 .1712 .1559 .1417 .1284 .1161 .1046 .0940	.1914 .1737 .1572 .1278 .1188 .1027 .0017 .0015	.1633 .1466 .1313 .1173 .1044 .0826 .0818 .0720 .0631	.1390 .1235 .1094 .0966 .0849 .0743 .0648 .0562 .0485
1.4988 1.5339 1.5693 1.6049 1.6408 1.6771 1.7136 1.7506 1.7879 1.8257	.31 .32 .33 .35 .35 .36 .37 .38 .39	.7703 .7632 .7762 .7492 .7492 .7593 .7584 .7215 .7146 .7078	.7088 .7001 .6914 .6828 .6742 .6656 .6571 .6486 .6402	.6243 .6139 .6029 .7923 .7818 .7713 .7510 .7708 .7406 .7306	.5332 .5206 .5083 .4960 .4540 .4721 .4603 .4487 .4373 .4260	.4449 .4311 .4176 .4044 .3766 .3661 .3538 .3418 .3300	.3644 .3701 .3361 .3225 .3092 .2963 .2837 .2714 .2794 .8478	.2939 .2558 .2564 .2264 .2269 .2148 .2052 .2052 .2052 .2052	.2339 .2201 .2069 .1943 .1821 .1705 .1594 .1487 .1385 .1288	.1839 .1711 .1589 .1173 .1363 .1276 .1179 .1065 .0977 .0893	.1431 .1314 .1204 .1101 .0012 .0327 .0747 .0672 .0603	.1103 .0999 .0902 .0812 .0786 .0576 .0578 .0512 .0121	.0841 .0751 .0667 .0590 .0590 .0455 .0396 .0343 .0294	.0636 .0778 .0488 .0483 .0367 .0313 .0266 .0223 .0166	.0477 .0411 .0352 .0299 .0252 .0210 .0174 .0141 .0113	.0354 .0300 .0301 .0309 .0311 .036 .0065 .0067
1.8640 1.9028 1.9421 1.9821 2.0226 2.0538 2.1057 2.1483 2.1918 2.2361	.41 .43 .44 .45 .46 .47 .48	.7000 .694g .6874 .6807 .6740 .6606 .6540 .6474 .6408	.6235 .6152 .6070 .5986 .5906 .5825 .5745 .5669 .5506	.5206 .5107 .5010 .4913 .4817 .4721 .4627 .4534 .4350	.k1k9 .4039 .3931 .3625 .3720 .3616 .3515 .3414 .3316 .3219	.3184 .3071 .2960 .2671 .2745 .2540 .2441 .2344 .2250	.2365 .2256 .2149 .2046 .1946 .1648 .1754 .1653 .1574 .1489	.1706 .1605 .1508 .1415 .1326 .1240 .1158 .1079 .1004	.1196 .11084 .1024 .0944 .0868 .0797 .0729 .0665 .0667	.0815 .0740 .0671 .0605 .0544 .0487 .0434 .0384 .0388	.0538 .0478 .0423 .0371 .0324 .0281 .0281 .0204 .0171	.0344 .0297 .0254 .0215 .0180 .0199 .0191 .0095 .0073	.0211 .0176 .0144 .0116 .0091 .0069 .0050 .0033 .0019	.0123 .0097 .0074 .0075 .0038 .0024 .0012 .0002 0007	.0067 .0048 .0033 .0020 .0009 0 0007 0012 0016 0019	.0032 .0020 .0009 .0000 0005 0010 0014 0018 0019

TABLE 3.- THE FUNCTIONS $\frac{dT_{k}}{d\tau}$ FOR AIR $(\gamma=1.4)$ FOR

SEVERAL VALUES OF THE INDEX k - Concluded

						Deran	ALI VALIDAS	OF THE IND	4 K - W	noluded						
		dY8.0	ax _{8.5}	ax _{9.0}	dYo s	ar _{10.0}	dT _{1.0.5}	4Y11.0	ar _{11.5}	a¥ _{12.0}	ay _{12.5}	dY12 A	ar _{13.5}	M14.0	ay _{14.5}	dT _{15.0}
) ×	i •	AT	<u>4</u> T	47	<u>ar_{9.5}</u>	<u>a+</u>	A7	- <u>11.0</u>	<u> </u>	47	17	dY _{13.0}	<u>ατ</u>	<u>a</u> T	4.5	<u>d</u> T
										<u> </u>			ļ <u>.</u>			
0.22473	0.01	0.9193	0.9138	0.9083	0.9028	0.8973	0.8918	0.8854	0.8809	0.8755	0.8701	0.8648	0.8595	0.8541	0.8489	0.8436
31944	-02	.8440	.8338	.8236	.8136	.8036	.7938	.7840	·7743	7617	-7553	-7459	.7366	7275	.7184	.7094
39324	.03	.7738 .7084	.7596	.7457 .6740	.7319 .6573	.7184	7051	.6920	6790	.6664	.6539 -5645	.6416	.6295 .5364	.6177	.6061	.5946 .4967
.45644		.6476	.6910			.6409	6250	.6093	-5941	.5791	.4860	.5503	4556	.5ee8 .4411	.5096	
.51299 .56493	.05 .06	.5911	.6276 .5690	.6081 .5476	.5891 .5269	-5707	-5527 -4877	.5353 .4691	.51.84 .4512	.5020 .4339	4172	4706 4012	3857	3708	1270	-4133
- 50493 51817	.07	5387	5150	.4922	4704	-5070 -4494	.4293	4100	.3916		3570	3409	.3051 .3254	.3106	.3565 .2965	.3427 .2829
.61347 .65938	80.	.4901	.5150 .4650	4415	.4190	3974	3769	3574	3389	•3739 •3213	.3045	.2886	2735	2592	2455	.2326
70321	.09	.4451	4195	3953	3723	3506	.3301	3107	12924	.2751	.2588	.2435	.2290	215	2025	.1904
74536	ài.	4035	-3775	3530	3301	3085	.2862	.2692	2515	.2348	.2192	.2046	.1910	1782	.1663	353
114250	'		1 '3'''	1,30,30	•35	""			'	"-5"		-2010			.2005	~~/,
.78612	u.u	.3651	-3390	.3146	.2919	-2707	.2510	.2326	-£155	-1997	-1649	.1712	.1585	.1468	.1358	.1257
.82572	.12	.3297	.3037		2574	2368	.2178	-2003	.1841	.1691	155	1427	.1310	1903	.1104	.1013
.86436	.13 .14	.2971	.2715	.2797 .2480	.2264	2066	.1884	.1718	.1566	1427	-1300	.1183	.1077	.0981	.0892	.0812
.90219		.2672	.2422	,2193	.1986	.1796	.1624	.1468	.1327	.1.198	.1082	-0977	.0881.	.0795 .0641	.0717	.0647
.93934	.15	.2397 .2345	.2154	·1934	.1736	.1557	1395	.1250	1119	1002	.0896	.0802	.0717	.06+1	-0573	.051.1
.97590	.16	.2145	.1911	1701	.1512	1311	.1194	1059	0940	.0833	.0739	.0654	.0579 .0465	.0513 .0408	.0454	.0402
1.0120	.17	.1915	.1690	-1/190	.1313	.1156	.1017	.0894	.0785	.0689	-0505	0531			.0357	.0313
1.0476	.18	.1704	.1490	.1302	.1136	-0990	.0862	.0750 .0627	.0553	.0567 .0463	-0493	.0427	.0371	.0322	.0279	.0241
1.0830	.19	.1513	.1310	.1133	-0978	-084	.0728		-0539		.0398	.0342	-0293	.0251	-0215	.0185
1.1180	.20	.1339	.11/48	.0982	.0839	.0716	.0617	.0520	.0442	.0376	.0319	.0271	-0230	.0195	.0165	.0140
1.1529	.ളൂ	.1181.	.1001	.0848	.0716	.0605	.051.0	.0429	.0361	.0303	.0254	.0213	.0178	.0149	.0125	.0104
1.1875	.22	.1038	.0870	.0728	.0609	.0507	.0423	0351	.0292	.0242	-0200	.0166	.0137	.0113	.0093	0077
1.2221	.23	.0909		.0623	.0514	.0423	.0348	.0285	.0234	.0191	.0156	.0127	.0104	.0084	.0068	.0055
1.2566	.24	.0793	. 0753 .0649	.0530	0431	-0351	.0284	.0230	.0186	.0150	-0120	0097	.0077	.0062	-0049	.0039
1.2910		.0688	0556	.0448	.0360	.0288	.0230	.0183	-0146	.0115	-0091	-0079	.0057.	.004%	.0035	.0027
1.3254	.25 .26	.0595	.0474	.0376	.0298	.0235	.0184	.0144	.0113	.0088	.0068	.0053	.0011	.0031	-00 <u>2</u> 4	.0018
1 3599	-27	.0511	·0 1 01	-0314	.0244	.0189	.0146	عدده.	.0086	.0066	-0050	.0038	.0028	.00e1	.0016	.0015
1.3944	.28	·0 ⁴ 37	.0337	-0259	.0198	-0151	-0124	.0086	-006∔.	-00\ _B	-0035	.0026	.0019	-0014	-0010	-0007
1.4291	.29	.0371	.0281	.0219	.0159	.0119	.0088	0065	10047	.0034	.0024	.0017	.0012	.0008	.0006	.0004
1.4638	.30	.0312	-0233	.0172	.0126	-0092	.0066	-0047	.0033	-0023	.0016	-0011	-0007	-0005	-0003	.0002
1.4988	31.	.0261	.0190	.0138	.0098	-0070	.0049	.0033	-0023	.0015	.0010	.0006	-0004	.0002	.0001.	0
1.5339	.32	.0216	01.54	8010	.0075	.0051	.0035	.0023	.0014	.0009	.0005	,0003	0001	0	0	l à l
1.7693	33	.0177	-0123	,008¥	.0056	.0037	.0023	.0014	.0008	·000 ¹	-0002	.0001	0	0001	0001	0001
1.5693 1.6049	33 31	-0143	.0096	.0063	.00¥0	.0025	-001.5	.0008	-0004	.0000	0	- 0001	0001	0001	0001	~.0001
1.6408	.35 .36	.0113	.0073	.0046	.0028	0016	.0008	.0003	.0001	0001	0002	0002	0002	0002	~-0001	0001
1.6771	.36	.0088	.0055	.0032	.001.8	.0008	.0003	0	0005	0002	0002	-,0002	0002	- 0005	~ .0001,	0001
1.7136	-37	.0067	.0039	-0021	,0010	-0003	-,0001	~.0002	0003	0003	0003	~.0002	- 0002	0001	0001	0001
1.7506	-38	.0050	10026	-0015	-0004	0001.	0003	0004	0004	0003	0003	0002	0002	0001	0001	0001
1.7879	-39	.0034	.0016	0005	000T	000k	0005	- 0005	0004	0003	0003	0002	0001	- 0001	0001	0 1
1.8257	-40	.0022	-0007	0001	0004	0006	0005	0005	0004	0003	0002	-,0002	0001	0001	0	٥
1.8640	. 4.3	.0012	.0001	0005	-,0006	0007	0005	- 0005	0004	0003	0002	0001	0001	0001	0	0
1.9028	.lig	+0004	- · 0004	0007	0008	0007	0006	0004	0003	000g	0002	0001	0001	0	õ	اقا
1.9421	.43	0003	0008	- 0009	0008	- 0007	0005	0004	0003	0002	0000	0001	0	ō	õ	ã
1.9821	.44	0007	0010	0010	0009	0007	0005	0003	~-000ē	0001.	0001.	0	0	0	٥	٥
2.0226	.45	~.0011	0015	0011	0008	0006	0004	0003	0002	0001	0001	0	0	0	0	0
2.0538		-,0013	0013	001.0	0008	0006	- 000	0002	0001,	0000T	0	0	0	0	0	0
2.1077	-47	0015	001.3	0010	0007	- 0005	-,0003	0002	0001	0	0	0	0	0	0	0
2.1483	-48	0015	0013	0009	0006	000k	0002	0001	~40001	0	0	0	o	Ď.	٩	º
2.1918	, <u>t</u> 9	0016	0012	0008	0005	- 0003	- 0002	0001	0	0	0	0	0	0	0	0
2.2361	.50	0015	~.0011	0007	-,0005	~.0003	0001	0	0	0	0	١,٠	0	0	٥	이
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PARLE 4. - THE PURCHISES AT FOR AIR (7 = 1.4) FOR

SEVERAL VALUES OF THE INDEX &

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₁₄	_	₫T-0.5	W_1.0	dY_1.5	ay_2.0	6 <u>7.2.5</u>	ax.3.0	₫¥-3.5	dr_4.0	4Y-4.5	av5.0	ar_5.5	ar_6.0	dY_6.5	47.7.0	αγ ₋₇₋₂	ax_8.0	ax_8.5
i		<u>a,</u>	αŦ	a+	đτ	ΔŦ	ΦŤ	άŦ	đτ	đ۲	ďτ	d*	4.7	đ٢	đ.T	E T	ΔT	ā T
0.22473	0.01	-0.9888	0.9752	-0.9225	-1.2340	-1.1556	-1.1548	-1.1238		-1.1147	-1.1161		-1.1230	-1.1278	-1.1332	~1.1390	-1.1450	-1.1513
31944	02	9777	9507		-1.3671		-1.3480	-1.2729		-1.2583	-1.2632		-1.2728		-1.2936	-1.3061	-1.3197	-1.3339
39324	.03	9566	9267 9030		-1.4551	-1.3657 -1.4251		1.5963	-1.4878 -1.7413	-1.4333		-1.4440 -1.6658	-1,4625 -1,7100	-1.4715 -1.7083	-1.4921 -1.7464	-1.5108 -1.766	-1.5342 -1.8050	-1.5578 -1.8373
51299	05	9556 9447	8796		-1.5437	-1.4573			2.0345	-1.862	-1.7062	-1.9322	2.0357	-2.0038	-2.0817	-2.0899	-2.1587	2.1929
55.93	.06	- 9339	8567		-1.5557	-1.4644	-2.1787		-2.3590	2.1000	-2.41.0		-2.4599	-2.3665	-2-3300		-2.6342	2.600
.61347	.07	- 9231	- 8341	5099	-1.5512	-1.4486	-2.3576	-1.9976	-2.7047	-2.3379	-2.8767		-2.9992	-2.7998	-3.1268		-3.2829	-3.2420
65938	.08	912h	~.8118		-1.5325		-2.5116	2.060		-2.5633	-3.4032		-3.6643	-3.2986	-3.9070	-3.6392	-4.1662	-3.9946
70321	.09	9018	7900	- 3913	-1.5016	-1.3566	-2.0403		-3.4138	-2.7628	-3.9848		+ 4773	-3.8 87	-1.8991	-4.3767	-5.3492	4.9286 -6.0454
.74536	-10	8913	7684	~-332*	-1.4604	-1.2043	-2.7506	-21-1405E	-3 - 7537	-2.9234	-4.5994	-3.6728	-5.5705	-4.4251	-6.1215	-5,2080	-6.8919	-0.0454
78612	.11	~.8809	7473	2816	-1.4101	-1.1969	-2.8257	-2.1161	4.0685	-3.0326	-5.2329	-3.9809	-6.3855	-4.9923	-7.5740	-6.0952	-8.8378	-7-3179
82572	.12	- 8705	7265	2300	-1.3522	-1.0962	-2.8707	-2.0501		-3.0790	-5. 86 03	-4.2183	-7.4725	-5-5052	9.2366	-6.9786	-11.2021	-8.6809
.86436	.13	- 8602	7060		-1.9876		-2.8871		+.5806	-3.0530		-4.3572	-8.5915	-5.9108	-11.0648		-13.9595	-10.0242
-90g19	.14 .15	- 8500 - 8398	6859 6661	0376	-1.2173 -1.1422		-2.8688 -2.8223		4.7591 4.0754	-2.9463 -2.7530		-4-3703 -4-2324	-9.6931 -10.7203	-6.1502 -6.1617	-12.9883 -14.9112	-8.3833 -8.6807	-17.0340 -20.2915	-11.1886 -11.9673
.93934 .97590	.16	8298	6467	- 0010	1.0631	592			+.9229	-9.4688	-7.7910		-11.6101	-5.8842	-16.7139		-23.5362	-12.1120
1.0120	.17	- 8198	- 6276	0028	9806	4486	-2.6116	1.1362		-2.0919	-7.9991		-12.2968		-18.2570	-7.8139	-26.5119	11.3453
1.0476	.18	8099	6089	.0368	- 8956	- 300	-2-5097		4.7931	-1.6925	-8.0500	-2.7110	-12.7137	-4.2400	-19.3864	-6.3832	-28.908	-9-3777
1.0830	.19	8000	5905	-0744	8084	1490		5316		-1.0630	-7.9243		-12.796	-2.7839	-19.9400		-30.3732	-5.9303 7600
7-7390	-20	7903	57 24	-1106	~.7197	-0045	-2.1701	1894	-4.3457	4176	-7.6061	6 576	-12.4856	8662	-19.7556	9556	-30.5286	7600
1.1529	.eı	7806	7547	.1443	~.6300	.1588	-1.9660	.1745	-4.0013	.3072	-7.0836	6847	-11.7291	1.5226	-18.6793	3.1908	-28.9922	6.3129
1.1875	.22	7710	5373	.1765	5398	3131	-1.7-15	5963		1.1035	-6.3492		-10.4850	4.3736	-16.5744	8.3261	-25.4019	15.3774
1.2221	.23	7615	5203	-2071	1193	.4664	-1.4987		-3.0796	1.9613	-5.4001		-8.7234	7.6584	-13.3302	14.4150	-19.4426	26.1059
1.2566	.24	7520 7127	- 5035	-2359	3591	.6177	-1.2398	1.357		2.8695	- 1.23BI		-6.A31L	11.3279	-8.8696		-10.8733	39 2334
1.2910	.25 .26	7334	4871 4711	.2631 .2687	2695 1809	.7663 9113	9668 68al	1.7667 g.1811	-1.8722 -1.1747	3.8156 4.7863	-2.8700		3,5996	15.3129 19.5244	-3.1576	29.0298 37.1969	.4461	53.5-17 68.8321
1 3500	.e7	7242	4553	3128	0934	1.0521	- 3878	2.5910		5.7673	-1.3073 kase	12.0174	2530 3.5785	23.8556	3.7935	45.6017	14.5309 31.2515	84.5276
1.3599 1.3944	.28	- 7150	4399	-3353	- 0074	1.1879	0863	2.9943		6.7438		14.1467	7.8448	26.1838	21.100		51.3187	99.7825
1.4291	.29	- 7060	- 4248	3563	.0768	1.3182	-2203	3.3869		7.7007	4.3651	16,2299	12,4792	32-3737	31.1613	61,8141	71.2766	113.7075
1 4638	30	6970	¥100	-3758	.1590	1.4425	.5298	3.7651	2-0705	8.6228	6.5024	18.2174	17.3994	36.2807	11.8725	68.8700	93.7020	125-3006
1 1988	31	6861	- 3932	3939	.2390	1.5602	8398	4.1954	2-9728	92950	8 27 20	20.000	22,7089	39-7572	22-9535	74.6852	116.2115	133.7100
1 5339	.32	6793	- 3813	1107	.3167	1.6710	1.148	4.4642	3.8449	10.3033		20.0590	27 6985	12.6467	64.0787	78.8469	138,4889	137.2516
1.5693	-33	~.6705	3674	.1661	.3918	1.7744	1.4536	4.7785	4.7368	11.0330	13.2164	23 1059	32.5-90	44.8087	74.8853	80.9566	159.2912	135.6313
1.6049	.34	- 6619	3599	- 4401	4642	1.8701	1.7533	5.0654	5.6187	11.6713	15.4348	24.2166	37 8335	16.1036	84.9828		177.5031	127 6757
1.6408	-35	6533 6448	- 3406 - 3277	. 4529 . 4645	.6003	2.0374	2.0456	5.3221 5.5463		12.2059		24.9946	12 5202	16.1073	93.9645		191.9689	112.7245
1.6771 1.7136	.36 .37	6364	3150	1719	.6637	2.1085	2.3286 2.6008	5.73 5 9		12.9220		25.4023	46.7758 50.4687	45.6140 43.6405	101.4200		201.5425	90.3253 60.3218
1.7506	. 38	6280	- 3027	4841	7240	2.1711	2 860	5.8892		13.0859		24.9862	53.4718		110.1777	50.0335	201.7923	22.8997
1.7879	-39	6197	2905	4921	.7510	2.2251.	3.1060	6,0048	9.5128	13.1112		24.1191	55.6669	35.9567	110.7683	34.4964	190.7052	-21.3786
1.8257	.40	6116	2789	-4991	-8347	2.2703	3 - 3362	6.0815	10.1676	12.9933		22 7969	56.9470		106 4386	15.9681	171.3075	-71.5550
المعددا	.4 <u>1</u>	6034	9674	.5050	.8850	2.3068	3.5498	6.1184	10.7203	12.7293	ac 81 ~~	01 018	57 0001	00 0707	100 0204	_E 0.670	162 2010	-106 0703
1.8640 1.90e8	.42	5951	2562	5099	.9319	2.3346	3.7455		11.1943	12.3183		21.0182 18.7903	57.2201 56.4120	28 2797 15 1939	94.2330	-5.2579 -28.7620	143.3019	-126.2723 -183.7915
1.9421	.43	- 5875	- 24-53	5138	9753	2.3538			11 5836	11.7612		16.1299	54.4687	6.0818	92.1730		61,8860	-242.0285
1.98e1	44	- 5796	- 2347	5167	1.0153	2.3644	4.0796		11.8830	11.0611	27.6506	13.0626	51.3591	-3.9087	66.8423	-80.3252	9-5737	-298.6106
2.0226	1.2	5718	- 2243	.5187	1.0517	2.3666	4.2163		12.0883	10.2226	27.2226			-14.5959	48.3974		-19.1221	-350.9541
2.0638	.46	5641	2045	5201	1.0847	2.3605	4.3320 4.4261		12.1963	9.2326 8.1396	26.4244			-25.7678		-133.1180	-112.7267	-396.3594 -432.1212
2.1483	48	5189	- 1950	5196	1.1101	2.3242	4.4983		12.1120	6.9540	25-2547 23-7161			-37.1854 -48.5877		-157.8592 -180.2737	-179.4194 -247.0770	-455.6520
2.1918	.49	- 5414	- 1857	5183	1.1627	2.2946	4.5485		11.9182	5.6476		-6.8799		-59.6971		199.4350	-313.3276	-164.6116
2.2361	-50	- 5340	- 1768	5160		2-2576	4.5764		11.6239	4.2542		-11.3835	9.6942			-814.4478	-375.5230	-457 0107
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PAGE 4.- THE NUMBER OF AT FOR MIR (7 = 1.4) FOR

SEVERAT, VALUES	OF THE THIRT	¥ -	Concluded

H	7	87_9,0 8.7	67_9.5 6.7	47 _{-10.0}	dΥ_10.5	47_11.0 4.7	47_11.5	dY_12,0	47_12.5 47	47_13_0 d7	dΥ_13.5	dΥ_14.0	<u>ат_34.5</u> ат	47_15.0
0.82473 .31,944 .39324 .47,644 .51299 .51347 .67938 .70321	3834888588	1.368 1.368 1.368 1.368 1.368 1.368 1.368 1.368 1.368 1.368 1.368	-1.16g -1.36g -1.6103 -1.9185 -2.3119 -2.8234 -3.4982 -3.799 -5.7832	-1.1710 -1.3859 -1.9652 -2.9822 -2.9408 -3.7123 -4.8067 -4.3770	-1.1779 -1.3968 -1.6678 -2.0084 -3.0184 -3.7588 -4.6069 -4.1773	-1.1848 -1.4188 -1.6971 -2.0565 -2.5208 -3.1389 -3.995 -3.995 -6.9938	-1.1919 -1.1298 -1.1217 -2.1059 -2.7939 -3.2366 -1.1213 -7.2834 -6.966	-1.1950 -1.1411 -1.1753 -1.1753 -1.1753 -1.1753 -1.1753 -1.1753 -1.1753 -1.1753	-1.4647 -1.4647 -1.7917 -2.2106 -2.7776 -3.4787 -1.4797 -7.6189	-1.2136 -1.4826 -1.6249 -9.26577 -2.8523 -3.6138 -4.6798 -6.2138	-1.000 -1.000 -1.000 -1.000 -1.000 -1.000 -1.000 -1.000 -1.000	-1.2284 -1.5193 -1.6937 -2.3809 -3.0243 -3.8912 -5.0937 -6.8287 -9.2469	-1.2359 -1.5382 -1.5252 -2.4411 -3.1204 -4.0379 -7.0980 -9.6967	-1.2435 -1.5573 -1.9656 -2.5032 -3.2206 -4.1959 -5.5568 -7.5279 -10.5183
.79536 .76618 .82572 .86436 .90219 .93534 .97590 1.0120 1.0476 1.0830	4 1444444	-7: 7:36 -9:36 -9:36 -9:	-6.9997 -8.6899 -10.6601 -12.7417 -14.7129 -16.2491 -16.9223 -16.2148 -13.5474 -8.5231	4.00 11.00 10.00 1	-7.9798 -10.2436 -19.9716 -16.0303 -19.1377 -21.8171 -23.3768 -23.3768 -19.3347	-9.6219 -13.1425 -18.645 -26.1925 -17.7268 -17.4451 -77.26317 -75.26317 -85.6198 -99.8961	-9.1090 -12.0154 -15.6602 -20.0130 -24.6869 -29.0169 -32.0366 -27.9316 -27.9316	-15.763 -15.763 -21.8859 -21.688 -62.3829 -10.73829 -10.73829	-16.3920 -14.0467 -18.8619 -24.6376 -31.6397 -38.40377 -38.3839 -44.6378 -38.3839 -60.6847	-12 -5637 -17 -5829 -86 -5950 -36 -5655 -56 -5656 -12 -5656 -12 -5656 -12 -5656	11.899 14.995 14.995 14.995 14.995 17.795 17.795 17.795	-13.5788 -90.1158 -90.5605 -16.7921 -70.7818 -101.4589 -148.4449 -801.0310 -896.6824 -304.6183	-13,5116 -19,0861 -27,0210 -37,7613 -51,213 -79,4006 -85,1860 -85,1860 -74,4613 -34,9832	-15,2661 -23,0359 -35,8054 -56,4056 -88,2732 -134,850 -198,1788 -276,7499 -562,7377 -138,8015 -476,0468
1.1150 1.1529 1.1875 1.2921 1.2566 1.2910 1.3554 1.5599 1.3599 1.3491 1.4638	* **********	-46,4068 -44,1689 -37,9796 -47,0778 -10,7680 11,6806 39,4157 72,7158 111,0947 159,1640 157,4798	.0169 27.6744 47.6962 70.4617 96.5296 124.4133 172.6634 179.8631 200.1864 206.8549	-69.6918 -66.3207 -57.7733 -37.6022 -1.9662 -77.1525 -1.6128 -1.57.1525 -1.547 -1.525 -1.547 -1.525 -1.547 -1.525 -1.547 -1.525 -1.547 -1.525 -1.547 -1.525 -1.547 -1.525 -1.547 -1.525 -1.547 -1.525 -1.547 -1.525 -1.547 -1.525 -1.547	1.8855 21.7264 48.7406 83.0866 124.2142 170.7083 280.1817 269.8381 313.9239 347.8227 366.6179	-103.6805 -96.3977 -79.5447 -43.8794 13.7215 99.6958 197.8087 388.5554 465.3568 618.1419 770.3341	5.7095 36.4778 36.4788 143.6788 215.9334 296.5789 382.5314 464.6721 534.1111 576.5849	-153.0820 -144.4625 -111.3600 -15.0435 590.0700 208.1033 696.8250 501.4435 117.6051 1140.2652	12.5070 66.6806 143.6364 245.0613 368.6324 673.3705 766.3353 881.3822	-24.6029 -210.0728 -151.9399 -34.1045 130.5410 188.2705 1818.8784 1696.3506 2177.6908 2602.4106	25.7902 113.8951 241.5805 413.0712 623.5413 859.8999 1098.8701 1303.1880 1468.3904 1419.6472 1619.6722	-327 -7650 -302 -6937 -200 -8294 8 -4501 372 -7532 849 -7479 1498 -9364 2273 -1519 3111 -8262 3913 -5827 4542 -5497	48.0736 189.6490 401.8951 689.0518 1042.6534 1435.4962 1817.6378 8114.5871 2229.4900 2050.4628 1463.7261	-176.0450 -172.1938 -274.3651 115.3795 729.6349 1680.4180 2700.6125 1114.7935 2712.4972 689.2374 7632.8312
1.4988 1.5339 1.5693 1.6049 1.6771 1.7136 1.7306 1.7879 1.6257	* ***********	241.3456 282.8595 319.0503 346.8595 363.55376 350.8386 317.0398 262.8123	226.8495 223.9571 205.7789 174-5579 125.7099 59.8081 -82.6569 -229.7530 -347.7239	478.2656 549.3694 603.7170 633.1540 598.11992 508.11863 376.8033 196.8119 -29.9790	363.8799 334.0864 272.3780 177.4547 41.8999 -127.2873 -328.2886 -773.88667 -773.9011 -1037.1477	908.k19k 1016.k809 1077.0713 1076.k17k 985.9135 805.8151 517.0488 128.9233 -373.2588 -997.0803	742.0836 436.6865 260.2278 8.2439 -318.1714 -710.7724 -1153.3213	1696.3287 1788.2893 1795.8903 1639.7974 1286.3755 718.2329 -90.5685	722.7366 428.6679 -14.9664 -609.7999 -1341.2397 -2175.794 -3058.7296 -3915.6969	2895.2650. 2970.5617 2710.1863 2114.9212 1062.2631 -470.9748 -2454.9272 -4811.3394 -7397.7980 -10006.8959	776.4769 90.5749 -972.498 -2274.8988 -3791.9499 -9415.6181 -6965.9186 -8901.9926 -9130.3247 -9288.9624	4829.0863 1986.9902 3634.9771 1823.7387 -927.2536 -1939.3340	372.3667 -1280.5066 -3486.6291 -6149.0087 -9064.3166 -11916.0367 -1282.8876 -1565.9731 -15736.1936 -13400.8052	7606.3707 6337.9463 3333.8916 -1080.8012 -7541.4786 -13600.8051 -24675.3518 -33811.5703 -41704.9314 -46785.4964
1.8640 1.9028 1.9421 1.9621 2.0226 2.0638 2.1077 2.1483 2.1918 2.2361	在每七年前4七年的S	43,3881 -154,6578 -296,4243 -449,5651 -601,9913 -748,7728 -882,3892	-788.9303 -857.1596 -894.1756 -893.9920 -850.2013 -760.4260	-98.4618 -600.0107 -922.4615 -1290.4448 -1367.6642 -1367.5463 -207.5463 -2227.4933 -2283.8051 -2227.4964	-1861.6598 -1475.5966 -1778.1861 -1670.7977 -1675.8506 -1739.8706 -1312.6797 -971.0830 -517.7937 36.4762	-1604 .3468 -2881 .1164 -2944 .9478 -3944 .5941 -4026 .5774 -4334 .5759 -4415 .4879 -4223 .9702 -3785 .1569 -2903 .2300	-8619.7720 -3006.5607 -3018.5314 -6798.0704 -6335.6697 -1611.9176 -629.9661 -584.0184 1579.9106 3483.4844	4982 0232 6256 2557 7524 5656 6264 2657 6264 6266 6264 6266 6266 5266 6266 5266 6266 5266	-7363 .9171 -7183 .6818 -1369 .8199 -3049 .5621 -1172 .7338 1277 .5217 -137 .6789 7261 .1069	i ' . i	-3170.0486 1247.9001 6705.8115 12681.2582 19292.1504 25314.1657 50219.0078	-6609,9669 -87135,8949 -6317,6985 -80121,4262 -11247,3319 1262,7629 16918,1651 34726,1878 93150,6864 70373,4736	-8884.7877 -1819.2819 7673.2803 19114.2565 31687.4667 \$1953.1999 \$1959.9765 61920.4650 63186.2958 97971.5756	47368.964 41874.0994 -8999.9622 -8470.7699 19792.1259 53746.4356 90773.6473 126696.4343 136717.7921 177267.9291

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